



# Using Dynamical Precursors for Statistical SSW Prediction

M. Jucker<sup>1</sup> and T. Reichler<sup>2</sup>

<sup>1</sup>Climate Change Research Centre, University of New South Wales, Sydney, Australia  
<sup>2</sup>Department of Atmospheric Sciences, University of Utah, Salt Lake City, USA

www.martinjucker.com @DrJucker martin.jucker@unsw.edu.au



## CONTEXT

- From previous SSW lifecycle and composite studies, we know that **Eliassen-Palm flux ( $F_z$ )** peaks and polar vortex sharpens prior to SSW onset<sup>1-15</sup>
- Linear wave theory: waves propagate towards higher **refractive index**<sup>1,16</sup>

$$n^2 = \frac{\bar{q}_\phi}{(\bar{u} - c)/a} - \left(\frac{k}{\cos \phi}\right)^2 - \left(\frac{af}{2NH}\right)^2$$

- First term is the only dynamical term. **Potential vorticity gradient** is most sensitive to changes (proportional to second derivatives)

$$\bar{q}_\phi = 2\Omega \cos \phi - \left[\frac{(\bar{u} \cos \phi)_\phi}{a \cos \phi}\right]_\phi + \frac{af^2}{R_d} \left(\frac{p\theta}{T} \bar{u}_p\right)_\phi$$

- We analyze CM2.1 data from a 10k-year coupled high-top simulation from *Horan and Reichler (2017)*.

## 1. SSW → E

First, we check the standard approach of compositing SSWs around the onset date.

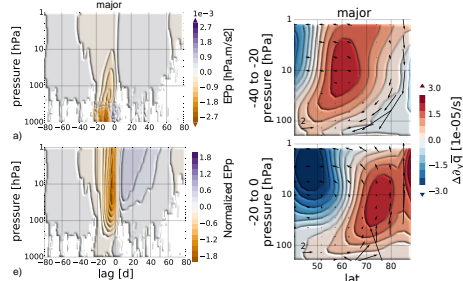


Figure: Example SSW composites for  $F_z$  (left) and  $q_{phi}$  (right) from *Jucker (2016)*.

This gives both a validation of the model data and an indication for relevant lead times for future prediction. We look for composite evolutions of  $F_z$  and  $q_{phi}$  similar to previous work, such as from *Jucker (2016)* above.

Indeed, our composites (right, w/  $1\sigma$  and 5<sup>th</sup>/95<sup>th</sup> percentiles) show that our GCM data agrees well with such composites:

- Strong increase of  $F_z$  (100hPa) within ~2 weeks, w/ peak ~1 week prior to onset (top).
- Weak but significant increase in  $q_{phi}$  (30hPa) ~1 month, and strong decrease ~1 week prior to onset (bottom).

Figure: SSW composites for  $F_z$  (top) and  $q_{phi}$  (bottom) from CM2.1: composite mean (thick continuous),  $1\sigma$  (shaded), 5%/95% percentiles around SSWs (blue dashed) and all days (black dashed). From *Jucker & Reichler (2018)*.

## REFERENCES

<sup>1</sup> Matsuno, 1971  
<sup>2</sup> Labitzke, 1977, 1981  
<sup>3</sup> Schoeberl, 1978  
<sup>4</sup> McIntyre, 1982  
<sup>5</sup> Limpasuvan et al., 2004  
<sup>6</sup> Polvani and Waugh, 2004  
<sup>7</sup> Scott and Polvani, 2004, 2006  
<sup>8</sup> Nishi et al., 2009  
<sup>9</sup> Ayarzagüena et al., 2011  
<sup>10</sup> Matthewman and Esler, 2011  
<sup>11</sup> Esler and Matthewman, 2011  
<sup>12</sup> Albers and Birner, 2014  
<sup>13</sup> Jucker 2016  
<sup>14</sup> Birner and Albers 2017

This work: Jucker and Reichler, "Dynamical Precursors for Statistical Prediction of Stratospheric Sudden Warming Events, submitted to GRL

## AIMS

- We invert the usual approach of first detecting all SSWs and then compositing
- Instead, we detect certain **events E** known to be precursors of SSWs and compute the probability that an SSW occurs within a given lead time
- Like this, the events become statistical predictors for the onset of SSWs in the future
- We want to quantify the information gain from using precursors as a function of lead time
- Precursor events are defined as the crossing of the 5<sup>th</sup> or 95<sup>th</sup> percentiles of
  - $F_z$ : upward EP flux at 100hPa ("**F event**")
  - $q_{phi}$ : meridional potential vorticity gradient at 30hPa ("**Q event**")

## RESULTS

- Anomalous strong  $F_z$  increases short-term SSW probability ~5x
- Anomalous weak  $F_z$  decreases short-term SSW probability >10x
- Anomalous strong  $q_{phi}$  decreases short-term SSW probability >10x
- Anomalous weak  $q_{phi}$  increases short-term SSW probability ~5x (first week)
- It also decreases long-term SSW probability ~2x (3-6 weeks)
- Anomalous strong  $F_z$  and weak  $q_{phi}$ 
  - increase immediate SSW probability ~10x (first week)**
  - decrease long-term SSW probability 2-5x (3-10 weeks)**

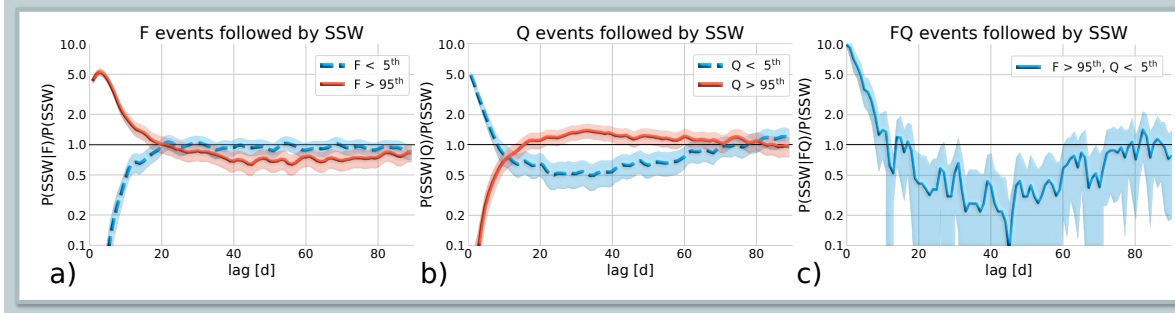


Figure: Conditional probabilities of SSW occurrence given an event E has happened,  $P(SSW|E)$ , divided by the climatological mean probability  $P(SSW) = 0.49\%/day$ . At long lead times, events and SSWs decouple, and  $P(SSW|E) = P(SSW)$ .

Strong upward EP flux at 100hPa increases the ~1 week SSW probability 5-fold, and strong negative EP flux anomaly reduces it ~10-fold (red/blue, left). Anomalous strong  $F_z$  also indicates slightly reduced  $P(SSW)$  between ~1-3 months.

Anomalous weak meridional PV gradient also increases immediate  $P(SSW)$  5-fold, and strong  $q_{phi}$  decreases it ~10-fold. In contrast to  $F_z$ ,  $q_{phi}$  also carries information about SSW occurrence out to ~60 days ahead, with  $P(SSW)$  about half the climatological value (blue dashed, middle).

Combining  $F_z$  and  $q_{phi}$  immediate  $P(SSW)$  increases ~10-fold, and decreases ~2.5 times on the monthly time scale all the way to ~10 weeks (right).

## 2. E → SSW

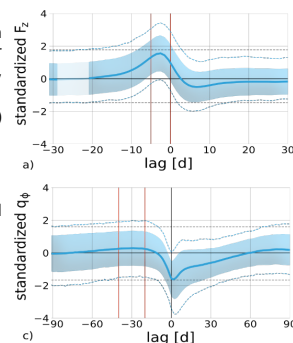
If we construct histograms of individual days rather than compositing all SSWs, we get one step closer to estimating how "generic" composite evolution really is.

The left figure shows histograms of all days (blue) or only the days within the lag intervals of any SSW marked with the red vertical lines on the far left (red).

The  $F_z$  distribution prior to SSWs is clearly different to the total distribution (top), with a strong shift towards positive (upward) values and a slight re-shaping of the tails (more Gaussian).

The  $q_{phi}$  distribution ~1 month before onset is also shifted towards positive numbers (sharper polar vortex edge, bottom). Note that while the PDF differences are much less pronounced than for  $F_z$ , the averaging period (lags -40 to -20) is also much longer (lags -40 to -20 for  $q_{phi}$  vs. -5 to 0 for  $F_z$ ).

Figure: Histograms of daily  $F_z$  (top) and  $q_{phi}$  (bottom) from CM2.1: All winter days (blue) vs. days associated with SSWs (red). For  $F_z$ , the red line includes days within lags -5 to 0, for  $q_{phi}$ , lags -40 to -20 prior to onset. From *Jucker & Reichler (2018)*.



Pushing the inversion further, we can also compare the fraction of SSWs preceded by a given event E (thick lines below) to the expected fraction of SSWs preceded by the same event, assuming E and SSWs are independent (thin lines). The difference between the two curves (shaded) gives a measure of the influence of event E on the occurrence of SSWs.

A much larger-than-random fraction of SSWs is preceded by strong  $F_z$  (top left), as well as weak  $q_{phi}$  (bottom left). 80% of all SSWs are preceded by  $F_z > 95^{th}$  percentile within 25 days, and  $q_{phi} < 0$  within 16 days.

$q_{phi} < 5^{th}$  percentile provides the strongest long term signal (purple, dashed).

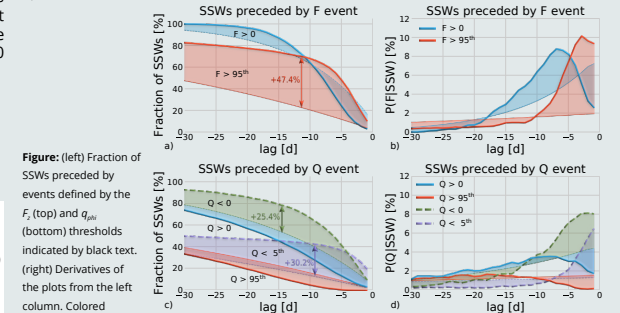


Figure: (left) Fraction of SSWs preceded by events defined by the  $F_z$  (top) and  $q_{phi}$  (bottom) thresholds indicated by black text. (right) Derivatives of the plots from the left column. Colored percentage numbers show the maximum differences between the actual and theoretical (if independent) SSW fractions. From *Jucker & Reichler (2018)*.

## ACKNOWLEDGMENTS

TR acknowledges support from NSF grant 1446292. MJ acknowledges support from the Australian Research Council (ARC) Centre of Excellence for Climate System Science (CE110001028), and ARC grant FL150100035 during the revision of this manuscript. This work used the xarray [https://xarray.pydata.org], parrmap [https://github.com/zeelio/parrmap], and aostools [https://github.com/mjucker/aostools] packages. We thank Eve Stavich from UNSW Stats Central for statistical support. We also acknowledge the Center for High Performance Computing at the University of Utah and the National Computational Infrastructure in Canberra for providing compute infrastructure and computing time.